

# Distributed Control in a Network of Households with $\mu$ CHP.

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## Abstract

This is an application of a dynamic price mechanism to distributed optimization of a network of houses which are both producers and consumers of electricity. One interesting candidate for domestic power generation is the Micro Combined Heat Power system ( $\mu$ CHP). In this device gas and power come together, and we are in particular interested in the electric output. We use a pricing mechanism based on dual decomposition, that was combined with feedback controllers in [1], and apply it to the modeling of the electrical power grid. In the end we perform a numerical test with realistic electricity demand patterns obtained from real data. Figure 1 shows promising numerical results; The demand in a cluster of 5 households is satisfactory followed by the unconstrained production.

The network of households is described by the dynamic equation  $x(t+1) = Ax(t) + Bu(t) + d(t)$ , where communication between neighbors is defined by system matrix  $A$ ,  $x(t)$  is the electricity balance information,  $u(t)$  is the controlled change in electricity production and  $d(t)$  is the change in electricity demand. A quadratic cost function is used to describe the performance.

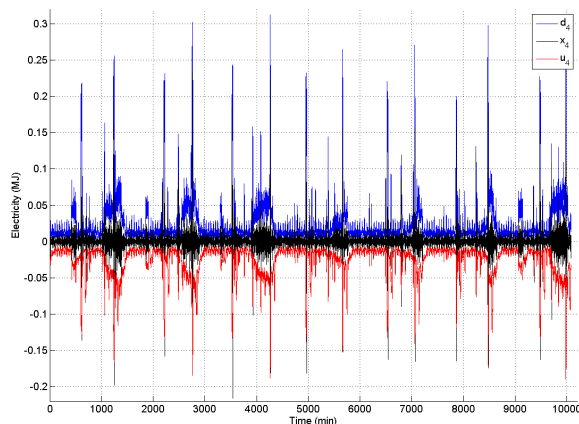


Figure 1: Simulation of five households connected in a chain. This means that price information is communicated to two direct neighbors. The blue line,  $d$ , is the realistic demand pattern obtained from field tests (TNO), the red line,  $u$ , is the controlled electricity production, and the black line,  $x$ , is the balance information that should go to zero.

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## References

- [1] Anders Rantzer. Dynamic dual decomposition for distributed control. In *Proceedings of American Control Conference*, St. Louis, June 2009.